8 Introduction to Functions

8–1 Equations in Two Variables

Objective: To solve equations in two variables over given domains of the variables.

Vocabulary

Ordered pair A pair of numbers for which the order of the numbers is important.

Solution of an equation in two variables An ordered pair of numbers that makes the equation true.

To solve an equation To find the set of all solutions of the equation.

Symbols (a, b) (The ordered pair a, b.)

CAUTION 1 (x, y) is not the same as (y, x); the order is important.

CAUTION 2 The equation 2x + 1 = 5 is a one-variable equation and has one number, $\{2\}$, for its solution. The equation 2x + y = 6 is a two-variable equation and will have pairs of numbers for its solution. The numbers in a solution pair of an equation in two variables are written in the alphabetical order of the variables.

Example 1	State whether	each ordered pair of	numbers is a solution	
	a. (1, 4)	b. (-1, 8)	c. (2, -2)	$\mathbf{d.}\left(\frac{5}{2},\ 1\right)$
Solution	Substitute eac	ch ordered pair in the	equation $2x + y = 6$	
	a. (1, 4) is a	solution because 2(1)	+ 4 = 6.	
	b. (-1, 8) is	a solution because 20	(-1) + 8 = 6.	
	c. $(2, -2)$ is	not a solution becaus	$e 2(2) + (-2) \neq 6.$	
	d. $\left(\frac{5}{2}, 1\right)$ is	a solution because 2(-	$\left(\frac{5}{2}\right) + 1 = 6.$	

State whether each ordered pair is a solution of the given equation.

2. 2x + y = 8(3, -2), (-3, -2) **3.** x + 3y = 6(3, 1)(-3, 3) 3. x + 3y = 61. x - y = 54. 12 - y = 2x(3, 6), (4, 4)(6, 1), (3, -2)**6.** 2x - 4y = 0 **7.** 3a - 4b = 125. 5x - 3y = 08. 2m - 3n = 6(3, 5), (-3, -5)(4, 0), (0, 3) (6, 2), (9, 4) $(2, 1), (1, \frac{1}{2})$ 12. 2xy = 4**10.** 5m - 4n = 119. 2x + 5y = 1811. xy = 8 $(3, 1), (2, \frac{1}{4})$ $(16, \frac{1}{2}), (-4, -2)$ $(\frac{1}{4}, 8), (-2, -1)$ $(4, 2), \left(\frac{3}{2}, 3\right)$ **13.** $x^2 + y^2 = 5$ **14.** $x^2 - y^2 = 10$ **15.** $x^2 - 2y^2 = 15$ **16.** $2x^2 + 3y^2 = 30$ (5, 5), (4, 1)(3, 2), (-3, 2)(2, -1), (3, -2)(3, -1), (1, -3)

8-1 Equations in Two Variables (continued)

Example 2	Solve $2x + 3y = 6$ for y in terms of x.
Solution	2x + 3y = 6 3y = 6 - 2x Subtract 2x from both sides of the equation. $y = \frac{6 - 2x}{3}$ Divide both sides of the equation by 3.

Solve each equation for y in terms of x.

7. $3x + y = 6$	18. $2x - y = 5$		19. $3x + 2y = 7$	
0. $x + 3y = 9$	21. $4x + 2y = 0$		22. $5x + 4y = 1$	0
Example 3	Solve $xy + x = 4$ if x and y are whole numbers.	x	$y = \frac{4-x}{x}$	Solution
Solution	1. Solve the equation for y in	0	denominator $= 0$	No
	terms of x. $y = \frac{4 - x}{x}$	1	$\frac{4-1}{1} = 3$	(1, 3)
	2. Replace x with successive whole numbers and find the	2	$\frac{4-2}{2} = 1$	(2, 1)
	corresponding values of y . If y is a whole number, you	3	$\frac{4-3}{3} = \frac{1}{3}$	No
	have found a solution pair. The solutions are $(1, 3)$,	4	$\frac{4-4}{4}=0$	(4, 0)
	(2, 1), and (4, 0).		ues of x greater than 4 e negative values of y .	10 Ten I deservation

Solve each equation if x and y are whole numbers.

23. $2x + y = 4$	24. $3x + y = 7$	25. $x + 3y = 6$	26. $x + 2y = 5$
27. $2x + 3y = 8$	28. $3x + y = 9$	29. $2x + 3y = 6$	30. $xy = 3$
31. $xy + 1 = 7$	32. $xy + 2 = 9$	33. $xy + y = 3$	34. $xy - 2y = 4$

Mixed Review Exercises

W	rite	each	number	in	scientific	notation.	
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1. 28,000,000	2. 0.00461	3. 104 million
4. 0.0000325	5. 37,000	6. 6,302,000

Simplify. Give answers in terms of positive exponents.

$7. \frac{1}{2n}$ $3. (2x)$ $3. \frac{1}{14x^2y}$ $10. \frac{1}{a^2}$	7. $\frac{4n^2}{2n}$	9. $\frac{42x^3y^2}{14x^2y}$ 10. $\frac{a^2}{a^2}$	8. $(2x)^{-3}$
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